

# Using Locata and INS for Indoor Positioning

Wei Jiang, Yong Li and Chris Rizos

School of Surveying and Geospatial Engineering  
University of New South Wales  
Sydney, Australia  
w.jiang@student.unsw.edu.au

Joel Barnes

Locata Corporation Pty Ltd  
Canberra, Australia

**Abstract**—In this paper, the authors describe the integration of an INS and the Locata system, that uses Locata’s position, velocity and attitude solutions to calibrate INS observations in order to achieve an accurate, robust and continuous indoor navigation solution. The multi-sensor experiment conducted at Locata’s Numerella Test Facility is described in the paper. The measurement data were collected and post-processed to evaluate the overall positioning performance and to analyse limitations of the integrated system. The test results indicate that Locata can be a substitute for GNSS, providing positioning services in severe multipath indoor environments, and the integrated system is capable of high accuracy, seamless navigation.

**Keywords**—Indoor positioning, Locata, INS, Multi-sensor integrated system

## I. INTRODUCTION

The Global Navigation Satellite System (GNSS) enables a significant improvement in positioning and navigation in open sky environments. Consequently many new application based on GNSS have emerged over the last few decades. The Inertial Navigation System (INS) is widely used in navigation applications. INS can provide motion information with a high update rate. However its navigation solution accuracy degrades quickly with time due to the sensor error accumulation. Therefore, the integration of INS with GNSS can calibrate INS sensor errors and ensure navigation solution performance with a comparatively high accuracy. In outdoor environments, GNSS/INS integration has demonstrated its capability of providing reliable 3D position, velocity and attitude solutions.

However, such technology is not possible for most indoor applications due to the severe signal obstruction of GNSS. This therefore has forced researchers to investigate alternative GNSS-like technologies with a view of replicating GNSS performance indoors. Locata is a ground-based navigation system which transmits ranging signals at frequencies in the 2.4GHz Industrial, Scientific and Medical (ISM) radio band. Such ranging signals from transceivers – known as LocataLites (LLs) – can be tracked by a Locata receiver. A Locata network – or LocataNet – contains at least four time-synchronised LLs (for 3D positioning) to cover an area with strong transmitted ranging signals. It has been shown that Locata can operate independently of GNSS and can achieve centimetre-level navigation accuracy when carrier phase measurements are measured and processed [1, 2].

In addition to the range measurements, Locata’s new correlator beamforming antenna, known as “TimeTenna”, now

is able to provide multipath-mitigated pseudorange, carrier phase and also azimuth measurements – pointed at the signal source. This beam direction is defined by the location of receiver and vehicle body frame [3]. In this paper, a 2D TimeTenna was used, which provided horizontal azimuth angle in addition to the traditional range measurements. The yaw angle could be resolved with such 2D azimuth angle measurements.

In traditional GNSS/INS integration a sole GNSS receiver can only provide position and velocity information, which is able to calibrate the position and velocity, as well as the roll and pitch angle. However, the yaw angle may be obtained with a lower accuracy compared with the other two attitude angles, because of its weak observability. Therefore, the contribution of this paper aims at achieving a more accurate and robust navigation solution by using integration concept. The authors integrate Locata and Inertial Measurement Unit (IMU) data using Locata’s position, velocity and yaw (PVY) solutions to calibrate IMU sensor errors. The assisted yaw angle integration is expected to give better INS bias calibration.

This paper is organised as follows. Locata measurement and model equations are introduced in section II. Then in section III, the integrated Locata/INS system is described. Finally, the field test is described, as well as the data analysis and evaluation.

## II. LOCATA MEASUREMENT AND MODEL FUNCTION

### A. Locata measurements

Similar to GNSS, the range measurements of Locata are of two types, pseudorange and carrier phase. The carrier phase measurements are more precise than pseudorange measurements. The basic Locata carrier phase observation equation between receiver A and LL channel  $i$  is:

$$\phi_A^i \cdot \lambda = \rho_A^i + \tau_{trop,A}^i + c \cdot \delta T_A + N_A^i \cdot \lambda + \varepsilon_\phi^i \quad (1)$$

where  $\phi_A^i$  is the integrated carrier phase observation in units of cycles,  $\rho_A^i$  is the geometric range from receiver A to LL  $i$ ,  $\lambda$  is the wavelength of the signal,  $\tau_{trop,A}^i$  is the tropospheric delay,  $c \cdot \delta T_A$  is the receiver clock error of receiver A,  $N_A^i$  is the carrier phase ambiguity, and  $\varepsilon_\phi^i$  are unmodelled residual errors. Note that there is no transmitter clock error presented in the

observation equation because of the tight time synchronisation of the LLs.

The receiver clock error may be estimated like GNSS single point positioning or eliminated using differencing. To eliminate the receiver clock the carrier phase measurements of the same frequency are single-differenced. When  $j$  is chosen as the reference signal, and  $i$  is another signal of the same frequency, the single-difference  $\Delta\phi_A^{ij}$  is:

$$\Delta\phi_A^{ij} \cdot \lambda = (\phi_A^i - \phi_A^j) \cdot \lambda = \Delta\rho_A^{ij} + \Delta\tau_{trop,A}^{ij} + N_A^{ij} \cdot \lambda + v \quad (2)$$

The unknown parameters are receiver coordinates  $(x_A, y_A, z_A)$  in the single-differenced geometric range  $\Delta\rho_A^{ij}$ .

### B. Ambiguity resolution

GNSS carrier ambiguities can be resolved by static initialisation or On-The-Fly (OTF) resolution techniques. The former idea is that the information content of carrier phase is a function of time which is directly correlated to the movement of GNSS satellites. As the GNSS satellites move in their orbits, the line-of-sight (LOS) vectors will have significant changes after many observation epochs, then the spatial diversity aids ambiguity resolution. However, this method is not suitable for Locata. In Locata applications, the LLs are fixed on the ground. For a stationary receiver, as the carrier phase measurement equations for different observation epochs are not independent of each other, the ambiguities cannot be computed by solving these equations. Therefore, if the static initialisation method is applied, the initial position of receiver needs to be known [4]. In the case of the OTF method it is able to realise ambiguity initialisation “kinematically”. For the Locata system, the kinematic mode provides the spatial diversity in the measurements, which makes the Locata OTF algorithm possible [5].

In the test case the Locata receiver remain static at a precisely surveyed point for a certain period of time. A Kalman filter is applied to estimate and “fix” the ambiguities. By smoothing the initial static data, the ambiguities can be obtained. Meanwhile in the Locata system, the ambiguities are “floating point” numbers. Once the float ambiguities are estimated with a certain level of accuracy, they can be treated as known parameters in (2).

### C. Iterative least squares estimation

Least squares estimation (LSE) is a common approach for obtaining a solution for a system which is used to estimate Locata receiver’s coordinates velocity and yaw angle.

#### 1) Position and velocity determination

The position measurement equation of the Locata is given in (1). Similar to GNSS, the Locata’s Doppler shift measurements are provided to calculate receiver’s velocity. The single-differenced measurement equation is obtained by time derivation of (2). Position and velocity can be computed by the linearised measurement equations:

$$\Delta\phi_A^{ij} \cdot \lambda - \Delta\rho_A^{ij} - N_A^{ij} \lambda = H_A^{ij} \cdot \delta x_A \quad (3)$$

$$\Delta D_A^{ij} \cdot \lambda = H_A^{ij} \cdot v_A \quad (4)$$

where  $H_A^{ij}$  is the single-differenced direction vector pointing from receiver to the LL,  $\delta x_A$  is the coordinate increment,  $\Delta D_A^{ij}$  is the single-differenced receiver Doppler shift, and  $v_A$  is the receiver’s velocity vector.

Applying LSE, for  $k$  single-differenced observations per epoch the error equation  $z = AX + b$  can be written as:

$$z = \begin{bmatrix} H_A & 0 \\ 0 & H_A \end{bmatrix} \cdot \begin{bmatrix} \delta x_A \\ v_A \end{bmatrix} + \begin{bmatrix} \Delta\phi_A \cdot \lambda - \Delta\rho_{A0} - N_A \lambda \\ \Delta D_A \cdot \lambda \end{bmatrix} \quad (5)$$

Single-differenced measurements of the same frequency are correlated because they have the common reference measurement. The covariance is therefore assumed to be half the variance [5]:

$$C = \begin{bmatrix} C_{\Delta\phi S1} & & & \\ & C_{\Delta\phi S6} & & \\ & & C_{\Delta D S1} & \\ & & & C_{\Delta D S6} \end{bmatrix}, C_* = \frac{\sigma_*^2}{2} \begin{bmatrix} 2 & 1 & \dots & 1 \\ 1 & 2 & \dots & 1 \\ \vdots & \vdots & \ddots & \vdots \\ 1 & 1 & 1 & 2 \end{bmatrix} \quad (6)$$

The weight matrix is  $P = C^{-1}$ .

The estimation of vector  $X$  is:

$$\hat{X} = (A^T P A)^{-1} A^T P b \quad (7)$$

#### 2) Yaw angle computation

The azimuth angle measurements using the TimeTenna antenna measures the angle that points to the signal source (LL) from the reference direction on the receiver’s body frame, see Fig. 1, where  $\Psi$  is the yaw angle of vehicle,  $\alpha$  is the measured azimuth angle.

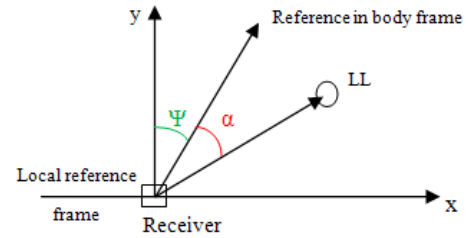


Figure 1. TimeTenna angle measurement

The yaw angle measurement equation is written as:

$$\alpha + \psi = \arctan\left(\frac{x_{LL} - x_R}{y_{LL} - y_R}\right) \quad (8)$$

where  $x_{LL}$  and  $y_{LL}$  are horizontal coordinates of LLs in the local reference frame, and  $x_R$  and  $y_R$  are horizontal coordinates of the receiver in the same frame.

### III. LOCATA/INS INTEGRATION

The Locata and INS sub-systems are loosely-coupled via extended Kalman filter (EKF). The EKF first makes a prediction based on the dynamics of the system, and later

corrects this prediction using measurements of the system [6]. In this section the authors describe how the EKF is applied in Locata/INS PVY integration. The INS error mechanism is used as the system model, and the Locata position, velocity and yaw angle are used as measurements.

The system model describes how the true state of the system evolves over time:

$$x_k = \Phi_{k-1} x_{k-1} + w_{k-1} \quad (8)$$

The true state  $x_k$  of the system at epoch  $k$  depends on the state of the previous epoch  $k-1$  and the system process noise. Matrix  $\Phi$  is state transition matrix. The vector  $w_{k-1}$  models the white noise in the system. The INS mechanisation errors can be modelled as:

$$\begin{bmatrix} \delta \dot{R}^n \\ \delta \dot{P}^n \\ \delta \dot{V}^n \\ \delta \dot{\omega}_g \\ \delta \dot{\omega}_a \end{bmatrix} = \begin{bmatrix} F_{RR} & F_{RP} & F_{RV} & C_b^n & 0_3 \\ 0_3 & F_{PP} & F_{PV} & 0_3 & 0_3 \\ F_{VR} & F_{VP} & F_{VV} & 0_3 & C_b^n \\ 0_3 & 0_3 & 0_3 & 0_3 & 0_3 \\ 0_3 & 0_3 & 0_3 & 0_3 & 0_3 \end{bmatrix} \begin{bmatrix} \delta R^n \\ \delta P^n \\ \delta V^n \\ \delta \omega_g \\ \delta \omega_a \end{bmatrix} + \begin{bmatrix} C_b^n & 0_3 \\ 0_3 & 0_3 \\ 0_3 & C_b^n \\ 0_3 & 0_3 \\ 0_3 & 0_3 \end{bmatrix} \begin{bmatrix} \omega_g \\ \omega_a \end{bmatrix} \quad (9)$$

where  $\delta R^n = [\delta\gamma \ \delta\theta \ \delta\psi]^T$ , components are the angular errors on the attitude  $\delta P^n$  and  $\delta V^n$  are position and velocity errors in local reference frame respectively;  $\delta \omega_g$  and  $\delta \omega_a$  are the gyro and the accelerometer biases respectively;  $\omega_g$  and  $\omega_a$  are the gyro and accelerometer noises respectively, which are assumed to be zero-mean Gaussian White noises;  $C_b^n$  is the attitude matrix, and  $F_*$  connects the sensor error sources and navigation solution errors. Details of the matrix can be found in [7].

The measurement model describes how measurements are related to the states:

$$z_k = H_k x_k + v_k \quad (10)$$

where  $z_k$  is the system input measurements, and the matrix  $H$  relates the current state  $x_k$  to the measurement  $z_k$ . The vector  $v_k$  models the measurement noises. The measurement model of the Locata/INS integration system can be written as:

$$\begin{bmatrix} P_{Locata}^n - P_{INS}^n \\ V_{Locata}^n - V_{INS}^n \\ \psi_{Locata}^n - \psi_{INS}^n \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & I_3 & 0_3 & 0_{3 \times 6} \\ 0 & 0 & 0 & 0_3 & I_3 & 0_{3 \times 6} \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \delta R^n \\ \delta P^n \\ \delta V^n \\ \delta \omega_g \\ \delta \omega_a \end{bmatrix} + v \quad (11)$$

where  $P_*^n, V_*^n, \psi_*^n$  are the position, velocity and yaw of the Locata and the INS respectively, with respect to the local reference system.  $v$  is characterised by measurement noise of the Locata system.

#### IV. TEST AND RESULT ANALYSIS

The indoor experiments were conducted in a metal shed at Locata's Numerella Test Facility (NTF), located in rural NSW, Australia. The shed was mostly empty with the exception of

some furniture and hardware tools placed near the walls, which can be seen in Fig. 2. This place is suitable for indoor testing because of the severe multipath environment. The LocataNet contains 5 LLs, which are installed in the corner of the shed. A Locata receiver was placed on a trolley with the TimeTenna also mounted on it [1].



Figure 2. Locata indoor test setup

By utilising the algorithm introduced in section II, difference between Locata's stand-alone solutions (position, velocity and yaw) and the reference are plotted in Fig. 3. The mean and standard deviation values are shown on Table 1. The reference is provided by Locata EKF solution with better than 2 cm positioning accuracy.

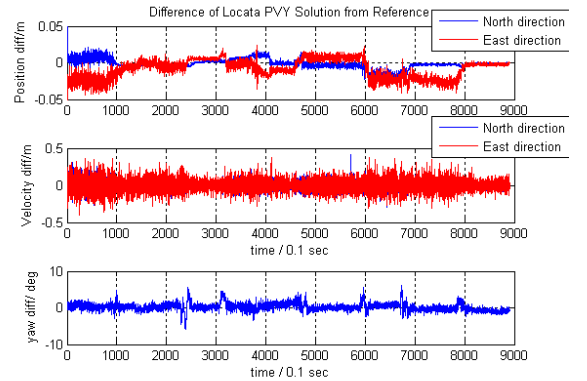


Figure 3. Difference of Locata position, velocity and yaw from reference

TABLE I. LOCATA PVY SOLUTION PERFORMANCE

|             | Position diff (m) |         | Velocity diff (m/s) |         | Yaw diff (deg) |
|-------------|-------------------|---------|---------------------|---------|----------------|
|             | North             | East    | North               | East    |                |
| <b>Mean</b> | -0.0014           | 0.0129  | 0.0554              | 0.0554  | -0.2519        |
| <b>Std</b>  | 0.0067            | -0.0080 | -0.0002             | -0.0002 | 1.0849         |

In order to investigate the navigation performance of the GPS/INS system, we have simulated INS data with different measurement quality. The IMU sensor may be categorised as commercial, tactical or medium, and navigation grades. As the accuracy of the yaw solution of Locata is about 1degree, we simulated the INS data for a commercial grade (e.g. Crossbow IMU400C) and tactical grade (e.g. Honeywell HG1700) IMU. The specifications associated with the accelerometers and gyroscopes errors are shown in Table II [8].

TABLE II. IMU LEVEL OF ACCURACY

| IMU     | Accelerometer |             |                                | Gyroscope             |             |                                      |
|---------|---------------|-------------|--------------------------------|-----------------------|-------------|--------------------------------------|
|         | Bias (mg)     | Scale (ppm) | Random Walk (mg/ $\sqrt{hr}$ ) | Bias ( $^{\circ}/h$ ) | Scale (ppm) | Random Walk ( $^{\circ}/\sqrt{hr}$ ) |
| IMU400C | 8.5           | $10^4$      | 5                              | 3600                  | $10^4$      | 0.85                                 |
| HG1700  | 1.0           | 300         | 0.25                           | 1                     | 150         | 0.125                                |

First consider the commercial grade IMU sensor. Fig. 4 and Fig. 5 depict the quality of the position, velocity and attitude solution of the integrated system when Locata PV and PVY are used as measurements, respectively. The standard deviations of navigation solution of the two integration strategies are compared in Table III.

TABLE III. STANDARD DEVIATION BASED ON PV &amp; PVY INTEGRATION

|          | Position error (m) |         | Velocity error (m/s) |          | Attitude error (deg) |        |        |
|----------|--------------------|---------|----------------------|----------|----------------------|--------|--------|
|          | North              | East    | North                | East     | Roll                 | Pitch  | Yaw    |
| Mean_PV  | -0.0015            | -0.0075 | -0.00003             | -0.00007 | -0.4199              | 0.3589 | 47.67  |
| Std_PV   | 0.04919            | 0.0624  | 0.1423               | 0.1737   | 0.4391               | 0.3612 | 119.71 |
| Mean_PVY | -0.0025            | -0.0080 | -0.0014              | -0.0003  | -0.4185              | 0.3715 | 0.2752 |
| Std_PVY  | 0.0311             | 0.0431  | 0.0570               | 0.0698   | 0.3057               | 0.2494 | 0.9303 |

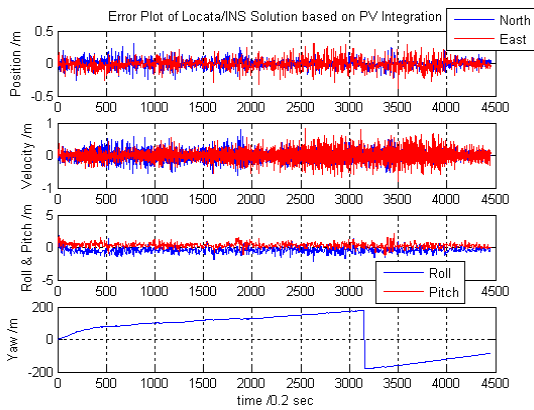


Figure 4. System error plot using PV integration

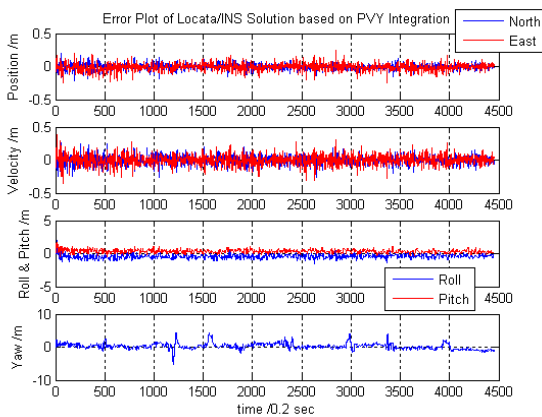


Figure 5. System error plot using PVA integration

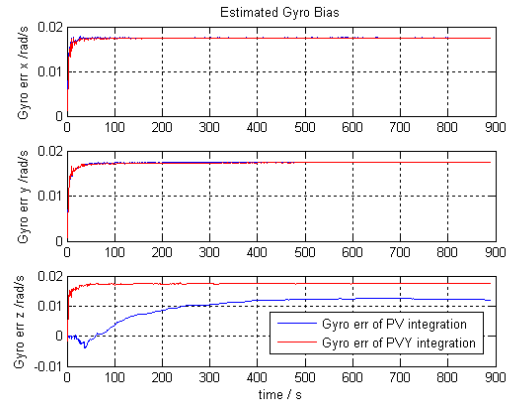


Figure 6 Gyro biases of two systems

As the result shown in Fig. 4, Fig. 5 and Table III indicate, adding yaw angle in the integration can increase the accuracy of the solution for the position, velocity or attitude components. In the PV-method, the yaw angle estimation is of poor quality. By comparing the gyro biases of the two integration systems in Fig. 6, one can see that in the PV-method the vertical direction gyroscope biases are not compensated for sufficiently in comparison with the PVY-method, which leads to the difference in yaw estimation accuracy for the two systems.

Compared with commercial grade IMU, the gyroscope bias of a tactical grade IMU is much lower, i.e.  $1^{\circ}/h$  in the simulation. The yaw angle error and estimated gyro bias based on the two integration systems are shown in Fig. 7. When operating in PV method, the gyro drift is nearly 0.25 degree in 900 seconds, which is less than the error of Locata's yaw solution. That explains the performance of the PV-method is better than the PVY-method. This result indicates that the PVY-method would be more suitable for circumstances when the gyroscope bias drift over a short time period is larger than Locata's yaw error.

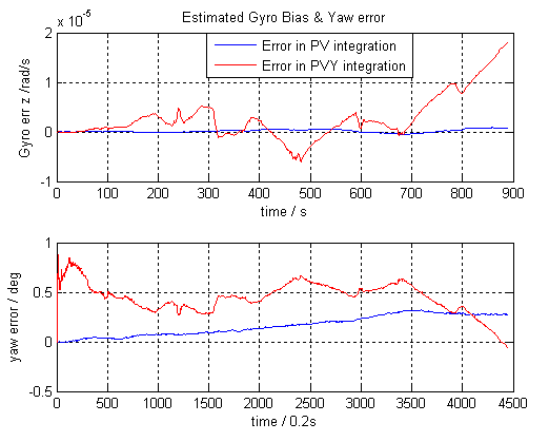


Figure 7 Estimated gyro biases and yaw errors of two systems

## V. CONCLUSION

In summary, a Locata/INS integration system is able to provide an accurate navigation solution that complements an

outdoor GNSS/INS system. Low-cost IMU sensors have comparatively high gyroscope biases which would result in a poor performance for the attitude solution, especially in the yaw direction. Utilisation of Locata's TimeTenna ensures measurement of a vehicle's yaw angle, which makes it possible to apply Locata/INS position, velocity and yaw integration. The adding of yaw calibration would better compensate the gyroscope bias in the vertical direction, which ensures a more reliable integration yaw solution. The preliminary results of the indoor experiment have shown that the integration system is able to provide an accurate and robust navigation solution. This confirms the proposition that Locata can be used as a substitute for GNSS for providing positioning services in severe multipath and/or indoor environments.

#### REFERENCE

- [1] Rizos, C., Roberts, G.W., Barnes, J., and Gambale, N.: Locata: A new high accuracy indoor positioning system. Proceedings of the Int. Conf. on Indoor Positioning & Indoor navigation (IPIN), Mautz, R., Kunz, M. & Ingensand, H. (eds.), Zurich, Switzerland, 15-17 September 2010, 441-447
- [2] Barnes, J., Rizos, C., and Kanli, M.: Indoor industrial machine guidance using Locata: A pilot study at BlueScope Steel. Proceedings of the 60th Annual Meeting of the U.S. Institute of Navigation, Dayton, Ohio, USA, 7-9 June 2004, 533-540.
- [3] LaMance, J., and Small, D.: Locata correlator-based beam forming antenna technology for precise indoor positioning and attitude. 24th Int. Tech. Meeting of the Satellite Division of the U.S. Inst. Of Navigation, Portland, Oregon, USA, 20-23 September 2011, 2436-2445.
- [4] Wan, X., Zhan, X., and Du, G.: Carrier phase method for indoor pseudolite positioning system. Applied mechanics and materials. 2011, 130-134, 2064-2067.
- [5] Bertsch, J., Choudhury, M., Rizos, C., and Kahle, H-G.: On-the-fly ambiguity resolution for Locata. Proceedings of IGNSS Symp., Surfers Paradise, QLD, Australia, 1-3 December 2009, CD-ROM procs.
- [6] Hide, C., Moore, T. and Smith, M., Adaptive Kalman filtering for low cost GPS/INS, Journal of Navigation, 2003, 56 (1), 143-152.
- [7] Angrisano, A.: GNSS/INS integration method. PhD thesis, Universita' Degli Studi Di Napoli "Parthenope", 2010.
- [8] Lee, J. K., and Jekeli, C.: Improved filter strategies for precise geolocation of unexploded ordnance using IMU/GPS integration. Journal of Navigation, 2009, 62 (3), 365-382